A&A manuscript no. (will be inserted by hand later)	ASTRONOMY
Your thesaurus codes are: 05 (10.07.2; 10.07.3: 47 Tuc; 08.16.4; 08.03.4; 08.13.2; 13.09.6)	ASTROPHYSICS

# Evolution of the dust mass loss with luminosity along the giant branch of the globular cluster 47 Tuc

A. Ramdani<sup>1,2</sup> and A. Jorissen<sup>2</sup> \*

<sup>1</sup> Département de Physique, Université d'Oujda, Maroc

Received / Accepted

Abstract. The present paper investigates the properties of the dust mass loss in stars populating the giant branch of the globular cluster 47 Tuc, by combining ISOCAM and DENIS data. Raster maps of 5 fields covering areas ranging from  $4\times 4$  to  $15\times 15\,\mathrm{arcmin^2}$  at different distances from the center of the cluster have been obtained with ISOCAM at  $11.5\,\mu\mathrm{m}$  (LW10 filter). The covered fields include most of the red variables known in this cluster. A detection threshold of about 0.2 mJy is achieved, allowing to detect giant stars at  $11.5\,\mu\mathrm{m}$  all the way down to the horizontal branch. No dust-enshrouded asymptotic giant branch stars have been found in the observed fields, contrary to the situation encountered in LMC/SMC globular clusters with larger turnoff masses.

The color index [12] – [2] (based on the ISO 11.5  $\mu$ m flux and on the DENIS  $K_s$  magnitude) is used as a diagnostic of dust emission (and hence dust mass loss). Its evolution with luminosity along the giant branch reveals that dust mass loss is only present in V3 (the only cluster Mira variable observed in the present study) and in V18, a star presenting intermittent variability. This conclusion confirms the importance of stellar pulsations in the dust formation and ensuing mass loss.

**Key words:** Globular clusters: 47 Tuc – Stars: AGB and post-AGB – circumstellar matter – Stars: mass loss – Infrared: stars

#### 1. Introduction

Stellar mass loss is an essential ingredient in the modelling of several important astrophysical processes. It plays a key role in the chemical evolution of the Galaxy, by returning to the interstellar medium the ashes of the nuclear-burning processes that took place during the star's lifetime. In Asymptotic Giant Branch (AGB) stars, the mass loss rate

 $Send \quad offprint \quad requests \quad to : \quad A. \quad Jorissen \quad email: \\ ajorisse@astro.ulb.ac.be$ 

is so large that the evolutionary timescale is controlled by mass loss rather than by nuclear burning. The general principles governing mass loss on the AGB are understood. Shock waves associated with the stellar pulsation push the gas far enough above the photosphere for dust to start condensing. Radiation pressure on the dust, when it couples to the gas, then provides the necessary thrust for matter to escape (e.g., Sedlmayr & Winters 1997). A parametrization of the mass loss rate on the AGB, in terms of the fundamental stellar parameters M, L, R and Z, is not available from empirical data (e.g., Zijlstra 1995), but Arndt et al. (1997) have proposed one based on computed models (see below). The oldest among empirical mass-loss-rate parametrizations is the Reimers formula (Reimers 1975; see Zijlstra 1995 and Sect. 11 of Habing 1996 for a discussion of the more recent parametrizations):

$$\dot{M}(M_{\odot} y^{-1}) = -4 \, 10^{-13} \, \eta \, \frac{(L/L_{\odot})(R/R_{\odot})}{(M/M_{\odot})},$$
 (1)

where  $\eta$  is a numerical factor [introduced later by Fusi-Pecci & Renzini (1976) and Mengel (1976)] of the order of unity. Although the Reimers formula provides a fair representation of the mass loss rates measured for G, K and (non-long-period-variable) M giants, it is well known that it predicts rates that are too low at the AGB-tip (e.g., de Jong 1983; Willson 1987; Bowen & Willson 1991; Blöcker 1995). The final AGB masses obtained with a mass loss rate following the Reimers prescription all the way to the AGB-tip are too large to satisfy the initial-final mass relationship of Weidemann (1987). Therefore, Renzini (1981) suggested the existence of a short episode of strong mass loss close to the AGB-tip (dubbed 'superwind'), with mass loss rates of the order of  $10^{-5}$  to  $10^{-4}$  M<sub> $\odot$ </sub> y<sup>-1</sup>, whereas the Reimers formula predicts maximum mass loss rates of the order of  $10^{-6} M_{\odot} y^{-1}$ . Luminous AGB stars with mass loss rates that large have since been found (e.g., de Jong 1983; Whitelock et al. 1991, 1994; Vassiliadis & Wood 1993 and references therein), as well as empirical evidences for a sudden increase of the mass loss rate at the end of the AGB (e.g., Delfosse et al. 1997 and references therein).

<sup>&</sup>lt;sup>2</sup> Institut d'Astronomie et d'Astrophysique, Université Libre de Bruxelles, CP 226, Boulevard du Triomphe, B-1050 Bruxelles, Belgium

<sup>\*</sup> Research Associate, F.N.R.S., Belgium

There has been much speculation concerning the nature and cause of the superwind. Willson (1981; her Figs. 5 and 6) and Bowen & Willson (1991) argued that pulsationdriven mass loss in Mira variables accounts for the required superwind. On the other hand, Netzer & Elitzur (1993) argued that the mass loss rate abruptly increases when the dust couples to the gas, thus causing the superwind phase. Detailed calculations of the AGB evolution, including all the ingredients (stellar structure, pulsation and shock waves, dust formation and coupling to the gas, radiative transfer) necessary to trigger mass loss in a selfconsistent way are now being performed for carbon-rich Miras (Fleischer et al. 1992; Höfner et al. 1996; Sedlmayr & Winters 1997; Winters et al. 2000) and reproduce the expected features of the superwind phase at the AGB-tip (Schröder et al. 1999). A parametrization of the mass loss rates, in terms of  $T_{\rm eff}$ , L and M, and based on the computed models, has been proposed by Arndt et al. (1997).

The sensitivity of mass loss to metallicity is one of the remaining question in the field. The low-metallicity behavior of dust- and pulsation-driven AGB mass loss has been investigated by Bowen & Willson (1991) with the conclusion that low-metallicity AGB stars reach the same mass loss rates than their higher metallicity counterparts, albeit at higher luminosities. This prediction is basically confirmed by observations of mass-losing AGB stars in the Magellanic Clouds, which do not call for low mass loss rates at low Z (see Zijlstra 1999 and Olofsson 1999 for recent reviews).

Giant stars in globular clusters are ideal targets to address these questions. In particular, the variation of mass loss with luminosity may be easily followed, the impact on mass loss of the pulsation properties of the long-period variables may be investigated, as well as the impact of the subsolar metallicity characterizing globular-cluster stars.

Among globular clusters, 47 Tuc (NGC 104) offers several advantages. It hosts many well-studied long-period variables (Sawyer-Hogg 1973, Glass & Feast 1973, Lloyd Evans 1974, Fox 1982, Frogel 1983), among which 4 Mira variables (V1 to V4) with periods ranging from 165 to 212 d, and visual amplitudes ranging from 1.5 to 4 mag. It is nearby (distance modulus = 13.7; Gratton et al. 1997) and has been the subject of many previous studies providing auxiliary data like bolometric magnitudes from UBVIJHKL fluxes or assignments of its giant stars to either the AGB or the RGB (Frogel et al. 1981). The basic parameters of 47 Tuc are as follows: [Fe/H] = -0.67, age  $\sim 10.5$  Gy (Gratton et al. 1997), turnoff mass  $\sim 0.9$  M<sub> $\odot$ </sub> (Hesser et al. 1987). Gillett et al. (1988) have performed a pointed observation of 47 Tuc with IRAS, and detected several sources at 12, 25 and 60  $\mu m$  (see Table 2). The use of ISOCAM onboard ISO (see Sect. 2) provides both a much better sensitivity (0.2 mJy instead of 10 mJy at 12  $\mu$ m) and a better angular resolution (a few arcseconds instead of 45 arcsec) than IRAS, and thus makes it possible to detect many more faint point sources than it was possible with IRAS.

The present study aims at monitoring the dust mass loss as a function of luminosity along the RGB and AGB in 47 Tuc. Relatively warm dust is easily detected from the flux excess that it produces at 12  $\mu$ m. Several authors (e.g., Whitelock et al. 1994, Le Bertre & Winters 1998, Jorissen & Knapp 1998) have shown that there is a tight correlation (at least for oxygen-rich stars in the solar neighbourhood) between the mass loss rate and the K-[12] color index, which may thus be used to trace the dust mass loss.

Another objective of the present study is to detect possible dust-enshrouded stars with no optical counterparts, as found by Tanabé et al. (1997, 1999) in globular clusters from the Magellanic Clouds.

#### 2. Observations

Mosaic images of 5 fields at different distances from the center of the 47 Tuc cluster have been obtained with the ISOCAM camera on board ISO (see Kessler et al. 1996; Cesarsky et al. 1996, for descriptions of ISO and ISOCAM respectively), using the LW10 filter (closely matching the IRAS  $12 \,\mu\mathrm{m}$  filter). The field positions have been chosen so as to survey most of the red variable stars in 47 Tuc. The Astronomical Observation Template (AOT) parameters for each of the fields are given in Table 1. They were adjusted so as to detect sources as faint as possible without saturating on the brightest sources. These contradictory requirements made us select a number  $N_{\rm obs}$  of elementary integrations as large as possible (namely  $N_{\rm obs} = 10$ , to keep within the total allocated time) but with short integration times  $(T_{\text{int}} = 2 \text{ sec})$  and low gain  $(\times 1)$ . With this setup, the detector saturates for fluxes of the order of 0.8 Jy/pixel, and remains linear up to about 0.3 Jy/pixel. The pixel field of view was taken equal to either 3'' (with the large field mirror) for the fields closest to the core, or 6" for fields farther out. The step size between two successive pointings of the mosaic was half the chip size (in either direction), i.e., 90" for the 6" pixel field of view or 45" for the 3" pixel field of view, to ensure 4 independent detections of the sources in the central region of the mosaic. The total integration time per source is therefore  $4 \times N_{\rm obs} \times T_{\rm int}$ . The very center of the cluster has not been observed to avoid saturation and crowding problems.

### 3. Reductions

## 3.1. ISOCAM image

The reduction of our ISOCAM data poses a special challenge as we are aiming at extracting sources as faint as possible in a field containing very bright (AGB) sources. Because of the strong detector memory effects, these sources will leave ghost images in the next pointings that ought not to be confused with faint sources. The PRETI routines

Table 1. Astronomical Observation Template parameters for the 47 Tuc observations (ISO program 'AJORISSE 47TUC')

Filter Date of observation	LW-10 (center $11.5\mu{\rm m}$ , range $8.0\text{-}15.0\mu{\rm m}$ ) $25\text{-}{\rm May}\text{-}1996$							
Field name	FIELD2	V5	FIELD3	FIELD4	FIELD1			
Planned targets	V3,V7,V11,V15,V18	V5	Lee #1421	V13	Lee # 5529			
Field center (J2000): $\alpha$	0h25m35s	$0\mathrm{h}25\mathrm{m}08\mathrm{s}$	0h22m46s	0h22m47s	0 h27 m0 s			
$\delta$	$-72^{\circ}04'30''$	$-72^{\circ}10'15''$	$-72^{\circ}18'00''$	$-72^{\circ}09'07''$	$-71^{\circ}55'00''$			
Distance from cluster center (arcmin)	6.9	7.2	14.5	7.4	16.7			
Detector gain	1	1	1	1	2			
Pixel Field of View (arcsec)	3	3	6	3	6			
Number of pointings	$9 \times 9$	$4 \times 4$	$9 \times 9$	$7 \times 7$	$8\times8$			
Total field of view (arcmin <sup>2</sup> )	$7.6 \times 7.6$	$3.85 \times 3.85$	$15.2 \times 15.2$	$6.1 \times 6.1$	$13.7 \times 13.7$			
Step between two pointings (arcsec)	45	45	90	45	90			

allowed us to overcome at least some of these problems. They were designed by Starck et al. (1999; see also Aussel et al. 1999) specifically for the detection of faint sources on ISOCAM images, after performing a careful removal of the cosmic ray glitches (both their short- and long-term effects) and correcting for the transient behaviour so as to provide a flat baseline.

The main steps of the reduction process are as follows. The default dark frame is first subtracted from the raw data (CIER files) using the CAM Interactive Analysis (CIA) package (Ott et al. 1997). The bad column 23 is replaced by the average of columns 22 and 24. The short-duration cosmic rays are identified from a  $3\sigma$  test on the short-term fluctuations of successive readouts and the affected readouts are masked. The long-term effects of cosmic rays are identified from their typical pattern in a multi-resolution median filter, and masked as well. Remaining long-term drifts (mainly due to the detector memory effect after passing on bright sources, and to the change of the ISOCAM configuration at the beginning of the observation) are suppressed by subtracting the baseline of each pixel's time history, obtained from the sequence of all the individual images.

The flat field is constructed from the median of the data themselves, since in the best cases, about  $800\ (\sim 10\times 9\times 9)$  readouts are available per pixel. The detector transient is corrected by the 'inverse method' developed by Abergel et al. (1996). In the present analysis, the fluctuations arising on top of the bright sources (probably caused by the jitter of the satellite) are often confused with short- term cosmic rays and unduly masked, resulting in a loss of useful readings for bright sources. This problem could possibly lead to underestimating the flux of bright sources, but the effect - if present - does not appear to be very severe, as will be seen from a comparison of our ISOCAM fluxes with previous IRAS measurements of the same sources (see Table 2).

The individual mosaic frames are then coadded into a single image. The source detection is performed on that image (Fig. 1) using a wavelet transform, which detects at each scale all pixels of the image above a given threshold  $\sigma$  of the noise map (Starck et al. 1999). A good compromise between maximum sensitivity and minimum number of false detections (as compared to optical sources; see Sect. 3.3) is obtained with a detection threshold set at  $5\sigma$ . More details about the criteria of inclusion of sources in the final source list are provided in Sect. 4.

The source fluxes are obtained by aperture photometry on the reduced image. The aperture used includes 12 pixels, and is the sum of the  $3 \times 3$ -pixels square centered on the source, plus 4 pixels exterior to this square and located in the middle of each side of the square.

The measured values were then multiplied by the factors 100/72 (for the fields observed with a 3" pixel field-of-view; see Table 1) or 100/84.5 (for the fields observed with the 6" pixel field-of-view) to account for

the point-spread-function (PSF) wing not falling on the selected aperture. Those factors were computed from the observed PSF provided by Okumura (ISOCAM PSF Report, 04/Nov/1998, available on the ISOCAM page http://www.iso.vilspa.esa.es/users/expl\_lib/CAM\_list.html).

The measured ADUs are converted to Jansky units using the conversion factor provided by the CIA software package (4.129 ADU/sec/mJy/pix). The uncertainty on the 12  $\mu$ m flux is the quadratic average of the Poisson noise on the signal, and of the uncertainty associated with the PSF correction (3%).

Because the reduction process is an intricated one implying many different steps, it is interesting to compare the ISOCAM fluxes with previous results obtained by Gillett et al. (1988) from pointed IRAS observations of 47 Tuc (Table 2).

The 12  $\mu$ m IRAS and ISOCAM fluxes generally agree within 25%, which is satisfactory considering the fact that the filters are not identical and that some of the LPV sources may be variable at 12  $\mu$ m as well. The largest deviations are obtained for the composite source V11+V18 (18%), and for V13 (31%). The 12  $\mu$ m flux of V13 is not reliable, as the ISOCAM image of V13 is in fact a blend of 3 different stars that are seen separately on the Digital Sky Survey image (Sect. 3.3). Another discrepancy concerns V7, which does not seem to have been detected by Gillett et al. (1988). This non-detection is surprising, since its flux at the time of our ISOCAM observation is similar to that of V15 which was detected by Gillett et al. (1988). A possible explanation would be that V7 was much fainter in the 12  $\mu$ m band at the time of the IRAS observation. This seems unlikely, however, since the ISOCAM flux for V7 agrees with the prediction for a dust-free photosphere (see Fig. 3), so that a smaller IRAS flux would mean that V7 was then underluminous at 12  $\mu$ m.

Note that the star V28 (= LR 5 = Lee #2758) is present on both FIELD3 and FIELD4. The ISOCAM fluxes from these two independent measurements differ by only 9% (Table 2), which provides an estimate of the internal consistency of the derived fluxes.

#### 3.2. DENIS data

As the  $K_s$  magnitude provided by the *Deep Near Infrared Survey* (DENIS; see Epchtein 1998) saturates at  $K_s = 6.5$  (Epchtein 1998), K magnitudes for the brightest sources detected on the ISOCAM images are taken from Frogel et al. (1981) or from Glass & Feast (1973). For the fainter sources, data from DENIS have been used, as published by Cioni et al. (2000) for fields around the Small Magellanic Cloud.

The cross-identification between ISOCAM and DENIS sources has been performed by overplotting their positions on the ISOCAM image. In most cases, an almost constant offset separated the positions of a given source in the two datasets. In some cases, however, an atypical off-

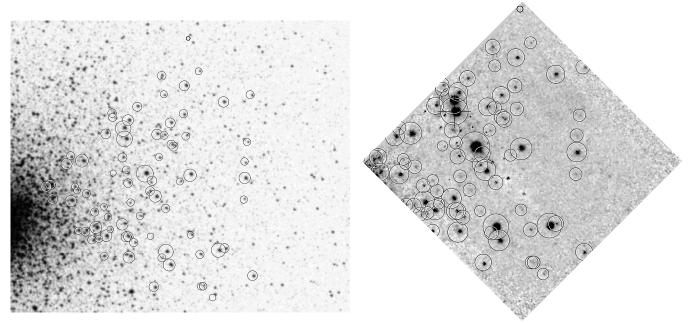


Fig. 1. Comparison of the Digital Sky Survey (left panel) and ISOCAM 12  $\mu$ m (right panel) images corresponding to FIELD2. The 12  $\mu$ m sources are identified by circles with a radius proportional to their 12  $\mu$ m flux (the variable V18 discussed in the text is identified by the cross on the right panel). East is to the right, North is up. The field size of the Digital Sky Survey image is  $12 \times 12$  arcmin<sup>2</sup>

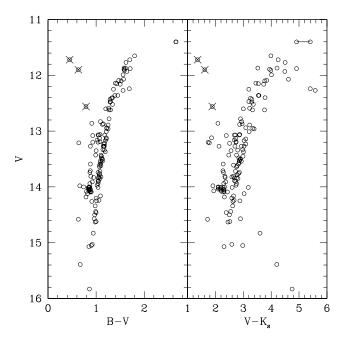
set whose origin is currently unknown had to be applied, especially for the brightest sources (V7 and V15). The cross-identification of these sources makes little doubt, as they generally correspond to the brightest sources in the area. Examples of cross identifications are listed in Table 2.

The variable V3 is the only one to vary by a large factor (about 4 mag in V and 0.5 mag in K; Sawyer-Hogg 1973, Frogel et al. 1981). The other variables have amplitudes smaller than 0.9 mag in V (Lloyd Evans 1974, Fox 1982). Therefore, they are not expected to vary by more than 0.1 mag in K. The average deviation  $K(\text{Frogel}) - K_s(\text{DENIS})$  is 0.21 mag (excluding V3).

#### 3.3. Optical data

Lee (1977) and Chun & Freeman (1978) provide UBV data for most of the fields surveyed by the present ISO-CAM observations. The assignment of a given giant star to either the RGB or AGB is possible from the (V, B-V) diagram presented in Fig. 2 for the stars detected at 12  $\mu$ m.

Optical images from the Digital Sky Survey were used to identify the optical counterparts of the infrared sources, along with the optical positions provided by Tucholke (1992) and its cross-identifications with the catalogues of Lee (1977) and Chun & Freeman (1978). The left panel of Fig. 1 identifies the 12  $\mu$ m sources on the optical image for FIELD2. Basically all sources brighter than V=14 (i.e.  $M_V<0.3$  for the distance modulus  $V-M_V=13.7$  of 47 Tuc) are detected at 12  $\mu$ m, corresponding to a complete-



**Fig. 2.** The (V, B-V) (left panel) and  $(V, V-K_s)$  (right panel) diagrams for the stars detected at 12  $\mu$ m and with B, V magnitudes available from Lee (1977) or Chun & Freeman (1978), and  $K_s$  from Table 3. The outliers (non-members?) 1321, 1412, 6209 are denoted by crosses

ness threshold of about 0.7 mJy including all the giants down to the horizontal branch (Fig. 2).

#### 4. Final ISOCAM source list and absence of dust-enshrouded AGB stars

The final list of ISOCAM 12  $\mu$ m sources obtained from the present observations (Table 3) has been obtained in the following way. A first list of candidate sources is provided by the 5  $\sigma$  detections as described in Sect. 3.1. Obviously spurious sources in that list, resulting from detector memory effects that were not totally eliminated by the reduction process, have been discarded. A few faint sources observed only on the ISOCAM images, but neither on the optical (Sect. 3.3) nor on the DENIS K images (Sect. 3.2) have been discarded as well. Table 3 lists the infrared sources, along with their optical identifiers, ordered by decreasing optical brightness.

The comparison of the optical images with our list of ISOCAM sources makes it possible to look for infrared sources with no optical counterparts. As can be seen on Fig. 1, there are none in FIELD2. The only source with no optical counterpart found in the present survey is the active X-ray galaxy X3 (Verbunt & Hasinger 1998) observed in FIELD3. Its 12  $\mu$ m flux amounts to 6.5 mJy.

One of the important results obtained by the present study is thus the absence of bright IR sources without optical counterparts, that could be associated with dustenshrouded AGB stars. This result may be used to set an upper limit to the lifetime of dust-enshrouded AGB stars. To do so, the number of horizontal-branch stars in the 529 arcmin<sup>2</sup> area covered by the fields listed in Table 1 is first evaluated. For that purpose, positions were taken from the catalogue of Tucholke (1992), with V and B magnitudes from Lee (1977) and Chun & Freeman (1978). Stars on the horizontal branch were selected on the basis of their magnitude and color index satisfying the conditions  $0.75 \le B - V < 0.94$  and  $13.9 \le V < 14.2$ . With 185 stars fulfilling these criteria, the fraction of obscured AGB stars to horizontal-branch stars turns out to be less than 1/185. Adopting  $1.23 \times 10^8$  y for the lifetime of stars with  $(M/M_{\odot}, Z) = (0.8, 0.004)$  on the horizontal branch (Girardi et al. 2000), this fraction turns into an upper bound of  $6.6 \times 10^5$  y for the duration of the obscured AGB phase. Extrapolating to the whole cluster the absence of obscured AGB stars in the surveyed fields does not make this limit much more constraining, since the catalogue of Tucholke (1992) contains only about twice more stars on the horizontal branch in the whole cluster. A limit of a few 10<sup>5</sup> v is not very meaningful, since the duration of the high mass-loss episode ("superwind") necessary to produce dust-enshrouded AGB stars appears to be of the order of a few 10<sup>4</sup> y, according to models of mass-losing AGB stars computed by Schröder et al. (1999). Observations of the structure of the CO shell around the post-AGB star AFGL 618 (Meixner et al. 1998) and around some OH/IR objects (Delfosse et al. 1997) point towards a duration of a few  $10^3$  y or even less for the superwind phase [the OH/IR objects observed by Delfosse et al. (1997) are,

however, probably rather massive (>  $5 M_{\odot}$ ?) and thus not representative of the AGB stars found in globular clusters].

The brevity of the corresponding evolutionary stage may not be, however, the only factor accounting for the absence of obscured AGB stars in 47 Tuc, since despite similarly adverse statistical expectations, Frogel et al. (1990) and Tanabé et al. (1997, 1999) nevertheless found such stars in three different globular clusters belonging to the SMC (NGC 419) or to the LMC (NGC 1783 and NGC 1978). These clusters belong to classes SWB IV-VI (Searle et al. 1980) and are characterized by turn-off masses 1.5 –  $1.6 \,\mathrm{M}_{\odot}$  (Nishida et al. 2000), much larger than the turnoff mass of 47 Tuc ( $\sim 0.9 \,\mathrm{M}_{\odot}$ ), and ages in the range 1.6 – 2.0 Gyr. The obscured AGB stars found by Tanabé et al. (1997, 1999) have  $M_{\text{bol}} = -4.9 - -5.0$ , somewhat larger than the bolometric magnitudes of the variable stars at the AGB tip in 47 Tuc, which have  $M_{\rm bol}$  between -3.4 at minimum and -4.7 at maximum (Frogel et al. 1981). The larger initial masses of AGB stars in the clusters where dust-enshrouded stars have been found is probably the key to the existence of such stars in the LMC/SMC globular clusters and not in 47 Tuc. Habing (1996) has reviewed the evidence indicating that larger initial masses imply higher mass-loss rates on the AGB, which in turn imply thicker dust shells [see e.g., Eq.(2b) of Le Sidaner & Le Bertre (1993) or Bedijn (1987)]. According to the spectral energy distributions computed by Bedijn (1987; his Fig. 4), dust-enshrouded stars have optical depths at 9.7  $\mu$ m in excess of  $\sim 5$ , and require mass loss rates in excess of about  $10^{-5} \mathrm{M}_{\odot} \mathrm{y}^{-1}$  (for typical values of the other relevant parameters), i.e., in the 'superwind' regime. Schröder et al. (1999) have shown that AGB stars with masses lower than  $1.1~{\rm M}_{\odot}$  never reach large enough luminosities to drive a dust-induced superwind, and thus have no chance to become dust-enshrouded. Finally, the luminosity function of obscured AGB stars in the field of the LMC rises steeply at  $M_{\rm bol} \sim -4.5$  (van Loon et al. 1999), which is about where the AGB ends in 47 Tuc (Frogel et al. 1981). Therefore, all available evidence points towards the low turnoff mass of 47 Tuc as being the main cause for its lack of dust-enshrouded stars, due to the absence of a superwind phase in low-mass AGB stars.

# 5. The F12/F2 index: dust mass loss as a function of luminosity

As indicated in Sect. 1, the ratio F12/F2 of the 12 to 2  $\mu$ m fluxes is expected to be a good indicator of dust mass loss. Fig. 3 presents the F12/F2 vs. K diagram for all the sources detected at 2 and 12  $\mu$ m. As indicated in Sect. 3.1, the error bars reflect the Poissonian noise on the signal, and the uncertainty on the PSF-wing correction. To fix the ideas, the F12/F2 ratio expected for dust-free stellar atmospheres has been estimated from the stellar atmosphere models of Plez et al. (1992) and

Bessell et al. (1998). Models of solar metallicity have been used, as only those are available over the whole temperature range covered by the observed stars. Nevertheless, a comparison between F12/F2 ratios obtained from ( $T_{\rm eff}=3800~{\rm K},~{\rm log}\,g=-0.5$ ) models of [Fe/H] = 0 and -0.6 (yielding F12/F2=0.046 and 0.045, respectively) reveals that metallicity has a negligible impact on the F12/F2 ratio (at least for those model stars with no mass loss).

The F12/F2 ratio for most of the stars is thus consistent with the value predicted for dust-free photospheres (Fig. 3). Only the bright LPV star V3 (the only Mira in Fig. 3, with P=192 d) and, more surprisingly the low-amplitude variable V18, do exhibit  $12~\mu m$  excesses. A marginal excess may be present as well for the irregular variable V11. The exact value of the excess is, however, difficult to assess for V3, as this Mira variable exhibits 0.5-mag variations in the K band (Frogel et al. 1981), and very likely varies as well in the  $12~\mu m$  band  $12~\mu m$  fluxes obtained at the same epoch, which is unfortunately not the case for the value displayed in Fig. 3. It is very likely, though, that V3 does exhibit at least some excess at  $12~\mu m$ .

The  $12\,\mu\mathrm{m}$  excess observed for V18 is more surprising (there is no doubt about its reality as may be assessed from Fig. 1), especially when compared to the absence of a similar excess for the stars V7 and V15, which are located slightly above V18 on the giant branch. The origin of the difference between the F12/F2 ratios of variable stars of comparable luminosities must probably be searched for in their variability properties. Both V11 and V18 are noteworthy in that respect. Fox (1982) notes that the irregular variable V11 possibly changed its period (and pulsation mode?) from about 100 d at the time of Lloyd Evans' observations (Lloyd Evans 1974) to 52 d about 10 y later. Similarly, Fox (1982) suggests that V18 may be of the type of variable that switches on and off intermittently. In the same vein, Tucholke (1992) lists two different Bmagnitudes for V18 (B = 17.4 and 13.5 for entries 2197 and 2198, respectively, which have exactly the same coordinates); they probably indicate that strong variations occurred over the time span covered by Tucholke's plates. It would be tempting to relate this behaviour with the sudden ejection of dust shells causing the star to brighten up at 12  $\mu$ m. A similar phenomenon has been proposed for semi-regular variable stars by Ivezić & Knapp (1999). Note that the large F12/F2 ratio of V18 cannot be ascribed to variations in the K band, since the  $K_s$  magnitude estimated from the raw DENIS frame<sup>2</sup> amounts to 7.33, as compared to 7.41 from the  $Two\ Micron\ All\ Sky\ Survey$  (Skrutskie 1997) and 7.44 obtained almost 20 y earlier by Frogel et al. (1981). Despite the fact that V28 is also suspected by Fox (1982) of being an intermittent variable, this variable star does not, however, show large excesses at 12  $\mu$ m (F12/F2 = 0.067 with K = 6.99 from Fox 1982).

Nevertheless, Fig. 3 shows that the dust mass loss does not increase gradually along the AGB, but that it appears suddenly as the AGB star becomes strongly variable. The mass loss rates of the dusty AGB stars in 47 Tuc is not expected to be quite large, though. A blind application of the empirical relationship between the mass loss rate and the K-[12] color<sup>3</sup> (Le Bertre & Winters 1998) yields a total mass loss rate lower than  $10^{-8}$  M<sub> $\odot$ </sub> v<sup>-1</sup> for V18! In fact, this relationship applies to solar-metallicity stars and to the regime of dust-driven winds, when the dust is abundant enough to couple to the gas. Neither condition is satisfied for the LPVs in 47 Tuc. Netzer & Elitzur (1993) have shown that the coupling between gas and dust is not achieved below mass loss rates of a few  $10^{-8} \text{ M}_{\odot} \text{ y}^{-1}$ (see also Fig. 20 of Jorissen & Knapp 1998). Such a low value for the mass loss rate of V18 is also confirmed by the application of a simple dust radiative-transfer model encapsulated in Eq. (6) of Frogel & Elias (1988, as corrected by Eq. (17) of Jura & Kleinman 1992). Adopting for V18  $F_{12}(\text{shell}) = 0.07 \text{ Jy (see Table 2, after subtraction of the}$ photospheric flux),  $v = 4 \text{ km s}^{-1}$  for the dust outflow velocity [according to Fig.B1 of van Loon (2000) for variable stars with short periods],  $T_{\rm eff} = 3680~{\rm K}$  and  $M_{\rm bol} = -2.96$ (Frogel et al. 1981) yielding  $R = 85 \text{ R}_{\odot}$ , and a grain cross section per unit mass  $\kappa = 2.3 \ 10^3 \ \mathrm{cm}^2 \ \mathrm{g}^{-1}$  at 12  $\mu \mathrm{m}$  for astronomical silicates with a density of  $3.3 \text{ g cm}^{-3}$  (Draine & Lee 1984) yields  $\dot{M} = \psi \ 2 \ 10^{-11} \ {\rm M}_{\odot} \ {\rm y}^{-1}$ , where  $\psi$ is the gas-to-dust ratio. With  $\psi$  of the order of  $10^3$ , as expected for envelopes with metallicities of 1/5 the solar value (solar-metallicity oxygen-rich envelopes typically have  $\psi \sim 200$ ; e.g., van der Veen 1989, Justtanont et al. 1994), a mass loss rate of the order of  $10^{-8}$  M<sub> $\odot$ </sub> y<sup>-1</sup> is indeed obtained. Incidentally, the K-[12] index of 1.37 for V18 appears quite small in comparison with mass- losing AGB stars in the solar neighbourhood, where K-[12] falls in the range 2-6 (corresponding to  $0.27 \le F12/F2 \le 11$ ).

 $<sup>^1</sup>$  Variations in the  $12\,\mu\mathrm{m}$  IRAS fluxes by factors as large as 1.6 have been reported by Jorissen & Knapp (1998) for some S-type Mira variables. The M-type Mira Z Cyg also exhibits variations by a factor of 2 at  $12\,\mu\mathrm{m}$  as revealed by ISO SWS spectra (Onaka et al. 1999). Finally, lightcurves in the N band of O-rich Miras (Le Bertre 1993) reveal variations by as much as 1 mag (i.e., a factor of 2.5). These variations may be accounted for by the underlying luminosity and temperature variations of the Mira variable.

 $<sup>^2</sup>$  Aperture photometry has been performed on the DENIS frame, and the zero-point has been estimated from a linear regression between the raw DENIS magnitudes and the K magnitudes from Frogel et al. (1981) for the stars in common between the two samples. The slope of the regression line amounts to 1.013 and the maximum relative deviation is 2%.

 $<sup>^3</sup>$   $K - [12] = -2.5 \log[(F_2/F_{12})(F_{12}(0)/F_2(0))]$ . In the definition of the color index K - [12],  $F_2(0) = 665$  Jy and  $F_{12}(0) = 28.3$  Jy are normalization factors ensuring that stars with no dust excess have K - [12] indices close to 0 (Fouqué et al. 2000; IRAS Explanatory Suppl., 1988)

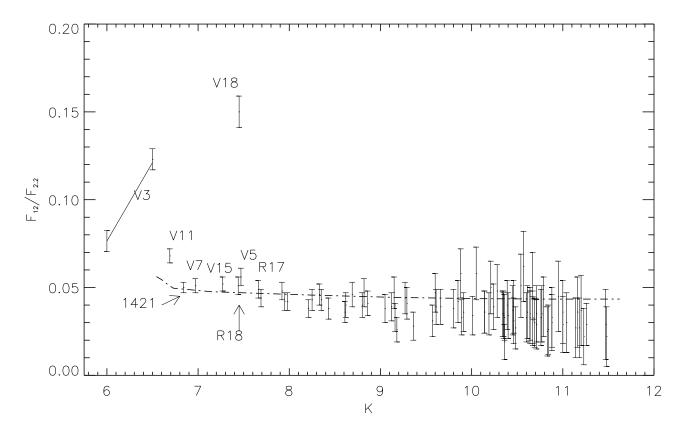


Fig. 3. The F12/F2 vs K diagram for stars detected at 2 and 12  $\mu$ m, with the variable stars identified. The conversion from K magnitudes to fluxes was performed by adopting a zero-magnitude flux of 665 Jy, following Fouqué et al. (2000). Note that the distance modulus of 47 Tuc is 13.7 (Gratton et al. 1997). The oblique segment for V3 translates its variability in the K band only (see Table 2), as existing data do not allow yet to estimate its variability range at 12  $\mu$ m. The dot-dashed line corresponds to the F12/F2 ratio derived from dust-free model atmospheres (see text)

This result is consistent with the conclusion of Sect. 4 that the low-mass AGB stars of 47 Tuc never reached luminosities high enough to trigger dust-driven winds.

In any case, the fact that 12  $\mu$ m-excesses are observed only for the LPV V3, for the intermittent variable V18 and possibly for the period-changing variable V11, is an indication that stellar pulsations play a key role in triggering dust mass loss. Frogel & Elias (1988) reached the same conclusion, based on the presence of 10  $\mu$ m excesses only in globular-cluster LPV stars and not in non-LPV cluster giants. The mass loss-pulsation connection is actually already well-documented, both on observational and theoretical grounds. A correlation between the mass loss rate and the pulsation period or amplitude of variation in the K band has been noticed by various authors (Whitelock et al. 1987, 1994 for O-rich Miras, Claussen et al. 1987 and Groenewegen et al. 1998 for C-rich Miras, Vassiliadis & Wood 1993 for a mixture of both). The various model

calculations of mass loss in AGB stars have also shown the key importance of pulsations for triggering the mass loss process (see the discussion in Sect. 1).

#### 6. Conclusion

The main results of the present study are (i) the absence of dust-enshrouded AGB stars in the surveyed fields, (ii) the existence of excess emission at 12  $\mu$ m due to circumstellar dust only for large-amplitude (or intermittent) variable stars.

The intermittent variable V18 appears to have an excess at 12  $\mu$ m much larger than stars of similar luminosities on the giant branch. A long-term monitoring of this star spanning several years and covering the optical and infrared bands would be of great interest to identify the origin of its anomalous properties.

Acknowledgements. M. Groenewegen is thanked for his help in the early phase of this project. D. Elbaz and H. Aussel provided invaluable help with the reduction of the data. The ISO-CAM data presented in this paper was analysed using CIA, a joint development by the ESA Astrophysics Division and the ISOCAM Consortium. The ISOCAM Consortium is led by the ISOCAM PI, C. Cesarsky.

#### References

Abergel, A., Bernard, J.P., Boulanger, F., et al. 1996, A&A 315, L329

Arndt T.U., Fleischer A.J., Sedlmayr E., 1997, A&A 327, 614 Aussel H., Cesarsky C.J., Elbaz D., Starck J.L., 1999, A&A 342, 313

Bedijn P.J., 1987, A&A 186, 136

Bessell M.S., Castelli F., Plez B., 1998, A&A 333, 231

Blöcker T., 1995, A&A 297, 727

Bowen G.H., Willson L.A., 1991, ApJ 375, L53

Cesarsky C., Abergel A., Agnese P., et al., 1996, A&A 315, L32

Chun M.S., Freeman K.C., 1978, AJ 83, 376

Cioni M.-R., Loup C., Habing H.J., et al., 2000, A&AS 144, 235

Claussen M.J., Kleinmann S.G., Joyce R.R., Jura M., 1987, ApJS 65, 385

de Jong T., 1983, ApJ 274, 252

Delfosse X., Kahane C., Forveille T., 1997, A&A 320, 249 Draine B.T., Lee H.M., 1984, ApJ 285, 89

Epchtein N., 1998. In: Epchtein N. (ed.) The impact of near-infrared surveys on galactic and extragalactic astronomy. Dordrecht, Kluwer (Astrophysics and Space Science Library), p.3 Fleischer A.J., Gauger A., Sedlmayr E., 1992, A&A 266, 321 Fouqué P., Chevallier L., Cohen M., Galliano E., Loup C., et al., 2000, A&AS 141, 313

Fox M.W., 1982, MNRAS 199, 715

Frogel J.A., 1983, ApJ 272, 167

Frogel J.A., Persson S.E., Cohen J.G., 1981, ApJ 246, 842

Frogel J.A., Elias J.H., 1988, ApJ 324, 823

Frogel J.A., Mould J., Blanco V.M., 1990, ApJ 352, 96

Fusi-Pecci F., Renzini A., 1976, A&A 46, 447

Gillett F.C., de Jong T., Neugebauer G., Rice W.L., Emerson J.P., 1988, AJ 96, 116

Girardi L., Bressan A., Bertelli G., Chiosi C., 2000, A&AS 141, 371

Glass I.S., Feast M.W., 1973, MNRAS 163, 245

Gratton R.G., Fusi Pecci F., Carretta E., Clementini G., Corsi C.E., Lattanzi M., 1997, ApJ 491, 749

Groenewegen M.A.T., Whitelock P.A., Smith C.H., Kerschbaum F., 1998, MNRAS 293, 18

Habing H.J., 1996, A&A Rev. 7, 97

Hesser J.E., Harris W.E., VandenBerg D.A., Allwright J.W.B., Shott P., Stetson P.B., 1987, PASP 99, 739

Höfner S., Feuchtinger M.U., Dorfi E.A., 1996, A&A 297, 815 Ivezić Ž., Knapp G.R., 1999. In: Le Bertre T., Lèbre A., Waelkens C. (eds.) Asymptotic Giant Branch Stars (IAU Symp. 191) San Francisco, ASP, p.395

IRAS Explanatory Supplement, 2nd edition, 1988. Joint IRAS Science Working Group. Washington DC, US GPO Jorissen A., Knapp G.R., 1998, A&AS 129, 363

Justtanont K., Skinner C.J., Tielens A.G.G.M., 1994, ApJ 435, 852

Jura M., Kleinman S.G., 1992, ApJS 79, 105

Kessler M.F., Steinz J.A., Anderegg M.E., et al., 1996, A&A 315, L27

Lee S.-W., 1977, A&AS 27, 381

Le Bertre T., 1993, A&AS 97, 729

Le Bertre T., Winters J.M., 1998, A&A 334, 173

Le Sidaner P., Le Bertre T., 1993, A&A 278, 167

Lloyd Evans T., 1974, MNRAS 167, 393

Meixner M., Campbell M.T., Welch W.J., Likkel L., 1998, ApJ 509, 392

Mengel J.G., 1976, A&A 48, 83

Netzer N., Elitzur M., 1993, ApJ 410, 701

Nishida S., Tanabé T., Nakada Y., Matsumoto S., Sekiguchi K., Glass I.S., 2000, MNRAS 313, 136

Olofsson H., 1999. In: Le Bertre T., Lèbre A., Waelkens C. (eds.) Asymptotic Giant Branch Stars (IAU Symp. 191). San Francisco, Astron. Soc. Pacific, p.3

Onaka T., de Jong T., Yamamura I., Cami J., Tanabé T., 1999. In: Cox P., Kessler M.F. (ed.) The Universe as seen by ISO. ESA-SP 427, p.381

Ott S., Abergel A., Altieri B., 1997. In: Hunt G., Payne H.E. (eds.) Astronomical Data Analysis Software and Systems VI. San Francisco, ASP conf. Ser. Vol. 125, p. 34

Plez B., Brett J.M., Nordlund Å, 1992, A&A 256, 551

Reimers D., 1975. Mem. Soc. Roy. Sc. Liège, 6e Ser., 8, p. 369 Renzini A., 1981. In: Iben I.Jr., Renzini A. (eds.) Physical processes in red giants. Reidel, Dordrecht, p. 431

Sawyer-Hogg H., 1973, Publ. DDO 3, No. 6

Schröder K.-P., Winters J.M., Sedlmayr E., 1999, A&A 349, 808

Searle L., Wilkinson A., Bagnuolo W.G., 1980, ApJ 239, 803 Sedlmayr E., Winters J.M., 1997. In: De Grève J.P., Blomme R., Hensberge H. (eds.) Stellar atmospheres: Theory and observations. Berlin, Springer Verlag, p. 89

Skrutskie M.F., 1997, Sky & Telescope 94, 46

Starck J.L., Aussel H., Elbaz D., Fadda, D., & Cesarsky, C. 1999, A&AS 138, 365

Tanabé T., Nishida S., Matsumoto S., et al., 1997, Nature 385, 509

Tanabé T., Nishida S., Nakada Y., Onaka T., Glass I.S., Sauvage M., 1999. In: Le Bertre T., Lèbre A., Waelkens C. (eds.) Asymptotic Giant Branch Stars (IAU Symp. 191) San Francisco, ASP, p.573

Tucholke H.-J., 1992, A&AS 93, 293

van der Veen W.E.C.J., 1989, A&A 210, 127

van Loon J.Th., 2000, A&A 354, 125

van Loon J.Th., Groenewegen M.A.T., de Koter A., Trams N.R., Waters L.B.F.M., Zijlstra A.A., Whitelock P.A., Loup C., 1999, A&A 351, 559

Vassiliadis E., Wood P.R., 1993, ApJ 413, 641

Verbunt F., Hasinger G., 1998, A&A 336, 895

Weidemann V., 1987, A&A 188, 74

Whitelock P.A., Pottasch S.R., Feast M.W., 1987. In: Kwok S., Pottasch S.R. (eds.) Late stages of stellar evolution. Kluwer, Dordrecht, p. 269

Whitelock P., Feast M., Catchpole R., 1991, MNRAS 248, 276 Whitelock P. Menzies J., Feast M., Marang F., Carter B., Roberts G., Catchpole R., Chapman J., 1994, MNRAS 267, 711 Winters J.M., Le Bertre T., Jeong K.S., Helling Ch., Sedlmayr E., 2000, A&A 361, 641

Willson L.A., 1987. In: Kwok S., Pottasch S.R. (eds.) Late stages of stellar evolution. Kluwer, Dordrecht, p. 253

Zijlstra A.A., 1995, ApSS 224, 309

Zijlstra A.A., 1999. In: Le Bertre T., Lèbre A., Waelkens C. (eds.) Asymptotic Giant Branch Stars (IAU Symp. 191). San Francisco, Astron. Soc. Pacific, p.551

A. Ramdani & A. Jorissen: Mass loss of giant stars in 47 Tuc

**Table 2.** Comparison of IRAS and ISOCAM 12  $\mu$ m fluxes. IRAS fluxes are from Gillett et al. (1988), and K magnitudes from Frogel et al. (1981), Glass & Feast (1973) or DENIS (Cioni et al. 2000). The variable name refers to Sawyer-Hogg (1973), and the four-digits number for non-variable stars refers to Lee (1977). The period P and visual amplitude  $\Delta V$  for the variable stars are taken from Sawyer-Hogg (1973) or Fox (1982)

Name	Alternate	F(	12) (Jy)		K		F12/F2	P	$\Delta V$	Rem.
	name	IRAS	ÍSOCAM	Frogel/Glass	DENIS	DENIS name	. ,	(d)	(mag)	
V3 V5 V7 V13		0.215 0.028 - 0.034	0.203 0.038 0.055 0.049:	$6.00-6.49\ 7.47\ 6.97\ 7.65$	7.35 6.79	J002501.97-720929.9 J002528.42-720652.2	0.08 - 0.12 $0.056$ $0.051$	192 45, 60–70 50–58 40	4.15 0.7 0.7 0.7	*
V15 V11 V18 V11+V18	W300 W12 L168	0.041 - - 0.235	$\begin{array}{c} 0.043 \\ 0.095 \\ 0.105 \\ 0.200 \end{array}$	7.27 6.69 7.45	7.03 6.48 - -	J002551.35-720703.8 J002506.64-720220.7 –	$0.052 \\ 0.068 \\ 0.150$	38 52:, 100	0.2 0.8 0.3	
$\begin{array}{c} 7701 \\ 8745 \\ 7701 + 8745 \end{array}$	R17 R18=V16	- 0.065	$0.028 \\ 0.036 \\ 0.064$	$7.66 \\ 7.44 \\ -$	7.43 7.08 –	J002532.43-721052.2 J002529.74-721118.4	$0.049 \\ 0.051$			
R19 V28 2620	LR5	$0.034 \\ 0.078 \\ 0.018$	0.032: $0.071$ $0.065$ $0.021$					40:	0.4	* FIELD3, * FIELD4
5529 6304 1421 1601 1603 1533		0.020 0.031 0.071 0.023 0.026 0.026	0.022 0.032 0.062 0.024 0.018 0.013	7.92 6.84 7.94	7.78 7.22 6.68 7.69 7.85 8.21	J002604.55-715324.6 J002738.23-715257.6 J002330.55-722236.5 J002401.03-721513.0 J002339.15-721639.9 J002357.90-721857.8	$\begin{array}{c} 0.048 \\ 0.038 \\ 0.050 \\ 0.044 \\ 0.042 \\ 0.038 \end{array}$			

Remarks:

V13: The ISOCAM image is a blend of 3 sources, as seen from the Digital Sky Survey image

R19: The ISOCAM image is a blend of 2 sources, as seen from the Digital Sky Survey image

1421: Lee (1977) suspects this star to be a LPV

V 28 = LR 5 = Lee #2758

Table 3. List of sources detected at 12  $\mu$ m. The first column provides the source identifier from Lee (1977), Chun & Freeman (1978) or Tucholke (1992) (the latter being referred to by 'tuc' followed by a 4-digit number). The next three columns list the V magnitude from Lee (1977) or Chun & Freeman (1978), the DENIS  $K_s$  magnitude (except for V3, where K is taken from Frogel et al. 1981), and the V-K index. The fifth column lists the magnitude at 12  $\mu$ m, derived from the flux in Jy (F12) using the relation [12] =  $-2.5 \log F$ 12/28.3. The F12/F2 ratio is listed next, with F2(Jy) = 665  $10^{-0.4K_s}$ . The uncertainty  $\sigma(F$ 12/F2) on F12/F2 is given in column 7, and includes only the uncertainty coming from F12 (see Sect. 3.1). Column 8 indicates the field number to which the star belongs, and the last column contains remarks (like non-membership, based on an outlying position in the (V, V) or (V1, V2, V3 diagrams)

Star	V	$K_s$	V - K	[12]	F12/F2	$\sigma(F12/F2)$	Field Number	
6304	8.51	7.22	1.29	7.35	0.038	0.003	F1	non member
1601	8.88	7.69	1.19	7.67	0.044	0.005	F3	non member
1533	10.09	8.21	1.88	8.36	0.038	0.005	F3	non member
d-502,V3	11.40	6.49	4.90	5.36	0.123	0.006	F2	
d-502,V3	11.40	6.00	5.40	5.36	0.076	0.003	F2	
d-230, V13	11.65	7.66	3.99	6.90	0.085	0.007	F4	
1412	11.72	10.36	1.36	10.64	0.033	0.013	F3	non member
8756, V5	11.72	7.47	4.25	7.17	0.056	0.005	F5	
7726, V15	11.77	7.27	4.50	7.05	0.052	0.004	F2	
d-596	11.87	8.35	3.52	8.35	0.043	0.006	F2	
2620	11.87	_	-	7.84	_	-	F4	
7701,R17	11.87	7.66	4.21	7.50	0.049	0.005	F5	
e-484	11.88	_	_	7.94	_	_	F2	
d-598,V7	11.88	6.97	4.91	6.78	0.051	0.004	F2	
1603	11.89	7.95	3.94	7.96	0.042	0.005	F3	
1321	11.90	10.28	1.62	10.18	0.048	0.015	F3	non member
5529	11.91	7.92	3.99	7.78	0.048	0.005	F1	
8745,R18	11.93	7.44	4.49	7.24	0.051	0.005	F5	
2758,LR5	11.94	_	-	6.50	_	-	F3	
2758, LR5	11.94	_	_	6.59	_	_	F4	
6747	11.99	7.98	4.01	8.01	0.042	0.005	F2	
2721	12.06	_	_	8.43	_	-	F4	
d-493,V18	12.07	7.45	4.62	6.08	0.150	0.009	F2	
e-558	12.08	_	_	8.42	_	-	F2	
d-509	12.09	8.25	3.84	8.26	0.043	0.006	F2	
2426	12.10	8.33	3.77	8.25	0.046	0.006	F3	
e-563	12.14	8.69	3.45	8.64	0.046	0.007	F2	
1510	12.15	8.61	3.54	8.81	0.036	0.006	F3	
1505	12.16	8.43	3.73	8.55	0.038	0.006	F3	
5312	12.16	-	-	8.36	_	-	F1	
2734	12.21	_	_	8.68	_	_	F4	
e-599	12.23	_	_	8.58	_	_	F2	
1421	12.24	6.84	5.40	6.65	0.050	0.003	F3	
6719	12.24	_	_	9.50	_	-	F2	

Table 3. (Continued).

Star	V	$K_s$	V - K	[12]	F12/F2	$\sigma(F12/F2)$	Field Number	
d-141	12.25	9.05	3.20	9.18	0.038	0.008	F4	
d-492,V11	12.27	6.69	5.58	6.18	0.068	0.004	F2	
6504	12.28	-	-	10.86	-	-	F1	
6764	12.30	-	-	8.75	-	-	F2	
1709	12.36	8.80	3.56	8.89	0.040	0.007	F4	
1709	-	-	-	9.24	0.029	-	F3	
1605	12.36	8.82	3.54	8.71	0.047	0.008	F3	
6527	12.39	-	-	9.02	-	-	F1	
e-538	12.40	8.62	3.78	8.68	0.040	0.007	F2	
1513	12.41	9.15	3.26	9.05	0.047	0.009	F3	
2525	12.43	9.12	3.31	9.22	0.039	0.008	F3	
5422	12.44	-	-	8.97	-	_	F1	
6768	12.47	9.27	3.20	9.25	0.044	0.009	F2	
5627	12.48	9.18	3.30	9.73	0.026	0.007	F1	
8740	12.52	9.16	3.36	9.43	0.033	0.008	F5	
e-487	12.54	-	-	8.99	_	_	F2	
6209	12.56	10.67	1.89	11.01	0.031	0.014	F1	non member?
d-571	12.59	9.36	3.23	9.81	0.028	0.008	F2	
1301	12.60	9.60	3.00	9.50	0.047	0.011	F3	
e-512	12.62	8.86	3.76	8.89	0.041	0.007	F2	
6732	12.62	9.29	3.33	9.35	0.041	0.009	F2	
5636	12.68	_	_	10.34	-	_	F1	
7723	12.75	_	_	9.64	-	_	F2	
6407	12.78	_	_	9.85	-	_	F1	
6408	12.78	_	_	9.75	_	_	F1	
6728	12.78	9.88	2.90	9.57	0.058	0.014	F2	
6519	12.81	_	_	9.62	_	-	F1	
1527	12.83	9.89	2.94	10.17	0.033	0.010	F3	
d-143	12.86	10.77	2.09	10.99	0.035	0.016	F4	
6717	12.87	9.91	2.96	10.12	0.036	0.011	F2	
2742	12.88	10.01	2.87	10.25	0.034	0.011	F4	
2742	_	_	_	10.16	0.037	-	F3	
2712	12.89	9.66	3.23	9.75	0.039	0.010	F4	
e-561	12.91	_	_	9.53	_	-	F2	
f-384	12.91	_	_	9.26	_	_	F2	
5427	12.92	_	_	10.04	_	_	F1	
1628	12.94	9.85	3.09	9.88	0.042	0.012	F3	
e-479	12.95	9.61	3.34	9.72	0.039	0.010	F2	
d-208	12.96	9.57	3.39	9.94	0.031	0.009	F4	
1604	13.01	9.80	3.21	9.95	0.038	0.011	F3	

Table 3. (Continued).

Star	V	$K_s$	V - K	[12]	F12/F2	$\sigma(F12/F2)$	Field Number
1518	13.06	10.19	2.87	10.42	0.035	0.012	F3
1708	13.07	10.21	2.86	10.03	0.050	0.015	F4
1708	-	-	-	10.04	0.050	_	F3
2604	13.07	10.39	2.68	10.45	0.040	0.014	F3
2741	13.07	10.35	2.72	10.56	0.035	0.013	F4
2741	-	-	-	10.49	0.037	-	F3
6524	13.08	-	-	10.19	-	-	F1
5530	13.08	-	-	10.60	-	-	F1
1319	13.08	10.69	2.39	11.08	0.030	0.014	F3
f-394	13.11	-	-	9.44	-	-	F2
e-525	13.11	-	-	10.29	-	-	F2
7707	13.12	11.26	1.86	10.67	0.029	0.012	F5
1629	13.13	10.40	2.73	10.64	0.034	0.013	F3
d-229	13.14	10.05	3.09	9.71	0.058	0.015	F4
f-804	13.14	-	-	9.53	-	-	F2
6403	13.16	-	-	11.29	-	-	F1
2643	13.16	10.48	2.68	10.97	0.027	0.012	F3
1316	13.17	10.14	3.03	10.32	0.036	0.012	F3
d-144	13.19	10.45	2.74	10.59	0.037	0.014	F4
e-576	13.20	11.46	1.74	10.42	0.111	0.040	F2
1309	13.20	10.46	2.74	10.55	0.039	0.015	F3
6531	13.21	-	-	11.32	-	-	F1
1422	13.21	11.43	1.78	10.81	0.077	0.033	F3
2739	13.22	10.71	2.51	10.91	0.035	0.016	F4
2739	-	-	-	10.71	0.042	-	F3
2428	13.23	10.14	3.09	10.32	0.036	0.012	F3
e-533	13.23	-	-	10.73	-	=	F2
d-504	13.23	-	-	10.25	-	-	F2
1602	13.24	-	-	10.56	-	-	F3
6727	13.27	10.34	2.93	10.56	0.035	0.013	F2
1506	13.27	10.24	3.03	10.33	0.039	0.013	F3
6739	13.27	10.57	2.70	10.15	0.062	0.020	F2
8735	13.27	11.14	2.13	11.66	0.027	0.017	F5
d-560	13.31	-	-	10.60	-	=	F2
1714	13.33	10.35	2.98	10.62	0.034	0.013	F4
1714	-	-	-	10.62	0.034	-	F3
6711	13.34	10.54	2.80	10.35	0.051	0.018	F2
1743	13.35	10.79	2.56	10.90	0.039	0.017	F3
6616	13.36	-	-	10.50	-	-	F1
2744	13.37	-	-	11.19	-	=	F4

Table 3. (Continued).

Star	V	$K_s$	V - K	[12]	F12/F2	$\sigma(F12/F2)$	Field Number
6740	13.37	-	_	10.26	-	-	F2
d-213	13.37	10.36	3.01	11.25	0.019	0.010	F4
6737	13.43	10.95	2.48	10.91	0.045	0.020	F2
2731	13.43	10.67	2.76	10.99	0.033	0.015	F4
1406	13.45	10.46	2.99	10.80	0.031	0.013	F3
d-567	13.45	-	-	10.67	_	-	F2
6623	13.46	-	-	10.90	_	-	F1
e-521	13.47	-	-	10.19	-	_	F2
5423	13.48	-	-	11.32	-	_	F1
8614	13.48	10.64	2.84	10.95	0.033	0.015	F3
2528	13.50	10.60	2.90	10.87	0.033	0.014	F3
2737	13.51	10.64	2.87	10.89	0.035	0.015	F4
2737	-	-	-	10.96	0.033	_	F3
1408	13.53	10.67	2.86	10.49	0.051	0.019	F3
1320	13.54	10.61	2.93	10.81	0.036	0.015	F3
1522	13.56	10.71	2.85	11.12	0.029	0.014	F3
6509	13.57	-	-	10.59	_	_	F1
5526	13.58	-	-	11.28	-	-	F1
d-207	13.59	10.76	2.83	11.04	0.033	0.016	F4
2531	13.59	11.31	2.28	10.96	0.059	0.027	F3
5527	13.60	-	-	10.63	-	-	F1
1723	13.61	10.96	2.65	10.83	0.048	0.021	F3
1703	13.62	10.84	2.78	11.36	0.026	0.014	F3
1703	-	-	-	10.88	0.041	-	F4
6758	13.64	-	-	11.25	-	-	F2
5645	13.64	10.88	2.76	11.17	0.033	0.017	F1
d-490	13.67	-	-	10.80	-	=	F2
6501	13.70	-	-	11.08	-	-	F1
6614	13.70	-	-	11.08	-	-	F1
6628	13.71	-	-	11.18	-	=	F1
2727	13.71	11.44	2.27	11.27	0.050	0.026	F4
6720	13.72	11.00	2.72	11.40	0.029	0.016	F2
2713	13.74	11.45	2.29	10.35	0.119	0.041	F4
d-514	13.74	10.88	2.86	11.26	0.030	0.016	F2
2519	13.76	10.93	2.83	10.63	0.056	0.022	F3
1407	13.78	11.00	2.78	11.19	0.036	0.018	F3
6715	13.81	11.16	2.65	11.35	0.036	0.020	F2
d-210	13.81	11.47	2.34	11.89	0.029	0.020	F4
1716	13.82	11.23	2.59	11.94	0.022	0.016	F4
6212	13.83	11.48	2.35	12.17	0.022	0.017	F1

Table 3. (Continued).

Star	V	$K_s$	V - K	[12]	F12/F2	$\sigma(F12/F2)$	Field Number
2722	13.84	11.16	2.68	11.10	0.046	0.022	F4
1504	13.84	11.08	2.76	10.94	0.049	0.022	F3
1607	13.85	11.04	2.81	11.40	0.030	0.017	F3
7734	13.87	-	-	11.49	-	-	F2
6744	13.89	11.20	2.69	11.36	0.037	0.020	F2
1423	13.90	11.17	2.73	11.12	0.044	0.022	F3
d-218	13.91	11.54	2.37	11.75	0.036	0.024	F4
6611	13.91	-	-	11.44	-	-	F1
6518	13.93	-	-	11.37	-	-	F1
6601	13.93	-	-	11.58	-	-	F1
1411	13.94	11.64	2.30	10.92	0.083	0.037	F3
1516	13.94	11.18	2.76	11.71	0.027	0.017	F3
6762	13.94	-	-	11.09	-	-	F2
8502	13.94	-	-	12.54	-	-	F3
e-522	13.95	-	-	11.97	-	-	F2
2650	13.97	11.23	2.74	10.53	0.081	0.030	F4
6648	13.98	-	-	12.02	-	-	F1
1614	13.98	12.07	1.91	11.76	0.056	0.037	F3
5424	13.99	-	-	11.94	-	-	F1
d-597	14.00	-	-	10.75	-	-	F2
5419	14.00	11.67	2.33	11.97	0.033	0.024	F1
8736	14.00	-	-	12.42	-	-	F5
2527	14.00	11.90	2.10	11.37	0.069	0.038	F3
1617	14.01	10.83	3.18	11.43	0.025	0.014	F4
2746	14.01	11.81	2.20	10.45	0.148	0.053	F3
1715	14.01	11.91	2.10	11.46	0.064	0.037	F4
1715	-	-	-	11.07	0.092	-	F3
1717	14.01	11.41	2.60	11.66	0.034	0.021	F4
1526	14.01	11.73	2.28	11.25	0.066	0.034	F3
2735	14.01	11.82	2.19	11.23	0.073	0.038	F4
1712	14.02	_	_	11.82	_	-	F4
6402	14.03	_	_	12.22	-	-	F1
2730	14.04	11.88	2.16	10.67	0.129	0.052	F4
d-212	14.04	11.94	2.10	11.57	0.060	0.036	F4
2622	14.04	11.75	2.29	11.02	0.085	0.040	F4
6610	14.05	_	_	13.25	_	-	F1
6633	14.05	_	_	11.26	_	-	F1
5642	14.05	11.74	2.31	11.51	0.053	0.031	F1
5628	14.06	-	-	12.56	-	-	F1
6630	14.06	-	-	11.82	-	-	F1

Table 3. (Continued).

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	,								
6511         14.06         -         11.08         -         -         F2           6510         14.07         -         8.97         -         -         F2           1315         14.07         1.24         11.35         0.087         0.047         F3           6516         14.07         -         -         11.04         -         -         F1           4-563         14.07         -         -         11.04         -         -         F2           6604         14.07         -         -         12.52         -         -         F1           1429         14.08         11.79         2.29         12.19         0.029         0.023         F3           1754         14.08         11.78         2.31         11.72         0.046         0.030         F1           4-249         14.09         11.66         2.43         11.54         0.047         0.028         F3           4-249         14.12         11.09         3.03         11.02         0.045         0.021         F4           4-389         14.12         11.09         10.47         -         -         F2           2747 <th>Star</th> <th>V</th> <th><math>K_s</math></th> <th>V - K</th> <th>[12]</th> <th>F12/F2</th> <th><math>\sigma(F12/F2)</math></th> <th>Field Number</th> <th></th>	Star	V	$K_s$	V - K	[12]	F12/F2	$\sigma(F12/F2)$	Field Number	
6511	1702	14.06	11.85	2.21	11.80	0.045	0.030	F4	
14-469	7717	14.06	-	-	11.08	_	-	F2	
14-469	6511	14.07	_	_	12.45	_	-	F1	
1315			_	_		_	_	F2	
6516							0.047		
14.07				_			_		
6604							_		
1429							_		
1754									
6603         14.09         -         -         11.35         -         -         F1           64200         14.09         11.78         2.31         11.72         0.046         0.030         F1           d-249         14.12         11.09         3.03         11.02         0.045         0.021         F4           d-489         14.12         -         -         10.47         -         -         F2           7739         14.13         -         -         11.14         -         -         F2           2747         14.16         11.51         2.65         11.49         0.044         0.026         F4           d-632         14.18         11.86         2.32         11.15         0.083         0.041         F5           1750         14.20         11.61         2.59         10.66         0.104         0.041         F3           6301         14.24         -         -         12.44         -         -         F1           1414         14.24         1.57         2.67         11.79         0.035         0.023         F1           2520         14.26         11.63         2.63         11.37									
5644         14.09         11.78         2.31         11.72         0.046         0.030         F1           d-200         14.09         11.66         2.43         11.54         0.047         0.028         F3           d-249         14.12         -         0.047         -         -         F2           7739         14.13         -         -         10.47         -         -         F2           2747         14.16         11.51         2.65         11.49         0.044         0.026         F4           d-632         14.18         11.86         2.32         11.15         0.083         0.041         F5           1750         14.20         11.61         2.59         10.66         0.104         0.041         F3           6301         14.24         -         -         12.44         -         -         F1           1414         14.24         11.57         2.67         11.79         0.035         0.023         F3           6612         14.25         11.63         2.63         11.37         0.054         0.030         F3           6524         14.29         -         11.66         - <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>									
d-200									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$									
d-489									
7739 14.13 11.14 F2 2747 14.16 11.51 2.65 11.49 0.044 0.026 F4 d-632 14.18 11.86 2.32 11.15 0.083 0.041 F5 1750 14.20 11.61 2.59 10.66 0.104 0.041 F3 6301 14.24 12.44 F1 1414 14.24 11.57 2.67 11.79 0.035 0.023 F3 6612 14.25 11.37 2.88 10.76 0.076 0.032 F1 2520 14.26 11.63 2.63 11.37 0.054 0.030 F3 6514 14.29 11.66 F1 1732 14.31 10.98 F3 6526 14.32 11.50 F1 6308 14.34 11.72 2.62 11.57 0.049 0.030 F1 2641 14.44 11.89 2.55 10.53 0.149 0.056 F3 8752 14.46 12.07 2.39 11.39 0.081 0.045 F5 5525 14.49 11.66 F1 1635 14.50 12.00 2.50 11.53 0.065 0.039 F3 8612 14.50 - 11.179 F1 1635 14.50 12.00 2.50 11.53 0.065 0.039 F3 8612 14.50 - 11.167 2.90 11.09 0.072 0.035 F5 1318 14.58 12.86 1.72 10.64 0.328 0.129 F3 1751 14.62 12.10 2.52 10.00 0.154 0.062 F3 6629 14.64 - 12.10 2.52 10.00 0.056 F3 673 14.69 1.218 2.45 11.24 0.101 0.052 F3 6630 14.48 11.82 - F1 6631 14.58 12.86 1.72 10.64 0.328 0.129 F3 1751 14.62 12.10 2.52 10.00 0.154 0.062 F3 6629 14.63 12.37 - F1 6733 14.96 10.83 - F1 6632 15.61 - 12.07 2.98 10.98 0.116 0.053 F3 6421 15.07 12.76 2.31 11.42 0.101 0.052 F3 6521 15.46 - 12.70 2.98 10.98 0.116 0.053 F3 6422 15.07 12.76 2.31 11.49 0.089 0.056 F1 1442251 - 10.00 - 11.69 0.009 0.006 F2 144234, 11.9 - 7.28 - 7.36 0.040 0.004 F4 non member									
2747         14.16         11.51         2.65         11.49         0.044         0.026         F4           d-632         14.18         11.86         2.32         11.15         0.083         0.041         F5           6301         14.24         -         -         12.44         -         -         F1           1414         14.24         11.57         2.67         11.79         0.035         0.023         F3           6612         14.25         11.63         2.63         11.37         0.054         0.030         F3           6514         14.29         -         -         11.66         -         -         F1           1732         14.31         -         -         11.50         -         -         F1           6526         14.32         -         -         11.50         -         -         F1           6308         14.34         11.72         2.62         11.57         0.049         0.030         F1           2641         14.44         11.89         2.55         10.53         0.149         0.056         F3           8752         14.49         -         -         11.66				-					
d-632									
1750       14.20       11.61       2.59       10.66       0.104       0.041       F3         6301       14.24       -       -       12.44       -       -       -       F1         1414       14.24       11.57       2.68       11.79       0.035       0.023       F3         6612       14.25       11.37       2.88       10.76       0.076       0.032       F1         2520       14.26       11.63       2.63       11.37       0.054       0.030       F3         6514       14.29       -       -       11.66       -       -       F1         1732       14.31       -       -       10.98       -       -       F3         6526       14.32       -       -       11.50       -       -       F1         6308       14.44       11.89       2.55       10.53       0.049       0.030       F1         2641       14.44       11.89       2.55       10.53       0.149       0.056       F3         8752       14.46       12.07       2.39       11.39       0.081       0.045       F5         5525       14.49       - <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>									
6301       14.24       -       -       12.44       -       -       F1         1414       14.24       11.57       2.67       11.79       0.035       0.023       F3         6612       14.25       11.37       2.88       10.76       0.076       0.032       F1         2520       14.26       11.63       2.63       11.37       0.054       0.030       F3         6514       14.29       -       -       11.66       -       -       F1         1732       14.31       -       -       10.98       -       -       F1         6526       14.32       -       -       11.50       -       -       F1         6308       14.34       11.72       2.62       11.57       0.049       0.030       F1         2641       14.44       11.89       2.55       10.53       0.149       0.056       F3         8752       14.46       12.07       2.39       11.39       0.081       0.045       F5         5525       14.49       -       -       11.79       -       -       F1         1635       14.50       12.00       2.50       10.53<									
1414									
6612         14.25         11.37         2.88         10.76         0.076         0.032         F1           2520         14.26         11.63         2.63         11.37         0.054         0.030         F3           6514         14.29         -         -         10.98         -         -         F1           1732         14.31         -         -         10.98         -         -         F3           6526         14.32         -         -         11.50         -         -         F1           6308         14.34         11.72         2.62         11.57         0.049         0.030         F1           2641         14.44         11.89         2.55         10.53         0.149         0.056         F3           8752         14.46         12.07         2.39         11.39         0.081         0.045         F5           5525         14.49         -         -         11.66         -         -         F1           5425         14.49         -         -         11.79         -         -         F1           5425         14.45         12.00         2.50         11.53         0.065									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$									
1732       14.31       -       -       10.98       -       -       -       F3         6526       14.32       -       -       11.50       -       -       F1         6308       14.34       11.72       2.62       11.57       0.049       0.030       F1         2641       14.44       11.89       2.55       10.53       0.149       0.056       F3         8752       14.46       12.07       2.39       11.39       0.081       0.045       F5         5525       14.49       -       -       11.66       -       -       F1         5425       14.50       -       -       11.79       -       -       F3         8612       14.50       -       -       11.15       -       -       F3         6631       14.54       -       -       11.93       -       -       F1         8731       14.57       11.67       2.90       11.09       0.072       0.035       F5         1318       14.58       12.86       1.72       10.64       0.328       0.129       F3         1751       14.62       12.10       2.52       10.7							0.030		
6526         14.32         -         -         11.50         -         -         F1           6308         14.34         11.72         2.62         11.57         0.049         0.030         F1           2641         14.44         11.89         2.55         10.53         0.149         0.056         F3           8752         14.46         12.07         2.39         11.39         0.081         0.045         F5           5525         14.49         -         -         11.66         -         -         F1           5425         14.50         12.00         2.50         11.53         0.065         0.039         F3           8612         14.50         12.00         2.50         11.53         0.065         0.039         F3           8612         14.50         -         -         11.15         -         -         F1           8731         14.57         11.67         2.90         11.09         0.072         0.035         F5           1318         14.57         11.67         2.90         11.09         0.072         0.035         F3           2652         14.63         12.18         2.45 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td>-</td><td></td><td></td></t<>							-		
6308       14.34       11.72       2.62       11.57       0.049       0.030       F1         2641       14.44       11.89       2.55       10.53       0.149       0.056       F3         8752       14.46       12.07       2.39       11.39       0.081       0.045       F5         5525       14.49       -       -       11.66       -       -       F1         5425       14.49       -       -       11.79       -       -       F1         1635       14.50       12.00       2.50       11.53       0.065       0.039       F3         8612       14.50       -       -       11.15       -       -       F3         6631       14.54       -       -       11.93       -       -       F1         8731       14.57       11.67       2.90       11.09       0.072       0.035       F5         1318       14.58       12.86       1.72       10.64       0.328       0.129       F3         1751       14.62       12.10       2.52       10.70       0.154       0.062       F3         2652       14.63       12.18       2.45									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5425	14.49	-	-		-	-		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			12.00						
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8612	14.50	-	-	11.15	-	-		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6631	14.54	-		11.93	-	-	F1	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	8731	14.57	11.67	2.90	11.09	0.072	0.035	F5	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1318	14.58	12.86	1.72	10.64	0.328	0.129	F3	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1751	14.62	12.10	2.52	10.70	0.154	0.062	F3	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2652	14.63	12.18	2.45	11.24	0.101	0.052	F3	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6529	14.64	-	-	12.37	_	-	F1	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	5421	14.78	-	-	11.82	_	-	F1	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	6733	14.96	-	-	10.83	_	-	F2	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			12.44	2.59		0.089	0.056		
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			-			-	-		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			_			_	_		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			_			_	_		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$						0.009	0.006		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$									
									non member
749 - 10.00 - 5.10 2.120 0.410 FO ACTIVE PARAXV	X3	_	13.35	_	9.10	2.126	0.416	F3	active galaxy